

## Question Bank for PG Course

### অঙ্ক (Mathematics)

অষ্টম (খ) পত্র (Paper-VIII B)

#### Graph Theory: PGM-T-VIII B

1. What is a simple graph?
2. What is the relation between the sum of the degrees of all the vertices  $\sum d(v_i)$  and the number of edges  $e$  of a graph?
3. How does a Digraph representing a reflexive binary relation be recognized?
4. Let  $G$  be a connected graph with  $n \geq 2$  vertices and  $e$  edges such that  $e < n$ . How many pendant vertices will be there?
5. Find the number of edges in a complete graph  $G$  with  $n$  vertices.
6. How many edges are there in  $K_{m,n}$ ?
7. State the necessary and sufficient condition for a complete graph  $K_n$  to be Eulerian.
8. Find the number of edges in a forest with  $n$  vertices and  $k$  components.
9. Which of the following statements is/are false?
  - i) A graph is a Tree if and only if it is minimally connected.
  - ii) Every pair of vertices in a Tree is joined by a unique path.
  - iii) A Tree with  $n - 1$  vertices contains exactly  $n$  edges.
  - iv) A connected graph with a cycle is called a Tree.
10. When is Kruskal's algorithm used?
11. What is the Height of a rooted tree?
12. What is the maximum number of vertices in an  $m$ -tree at level  $p$ ?
13. Find the relation between the height  $h$  and the number of vertices  $n$  of a complete binary tree  $T$ .
14. If  $G$  is a connected planar graph with  $n$  vertices,  $e$  edges and  $f$  faces, then write down Euler's formula.
15. Let  $G$  be a connected 4-regular planar graph with 8 vertices. How many faces does  $G$  have?